



## POWERS SQUARES OF INTEGERS

## PICK AND MIX [CALCULATOR ALLOWED]

Ref: G1C1. **1E1**

<p><b>A1</b> What digits can a square number end with?</p>	<p><b>A2</b> Find three square numbers which add together to make 142</p>	<p><b>A3</b> Which two <b>consecutive</b> square numbers have a difference of 17</p>	<p><b>A4</b> Two <b>different</b> square numbers are added together to make an even number between 50 and 100. How many ways are there to do this?</p>
<p><b>B1</b> Split the numbers below into three groups so that each group adds up to a different square number:  2, 2, 3, 3, 3, 3, 4, 4, 5, 5, 5, 6</p>	<p><b>B2</b> All square numbers greater than one can be made by adding two prime numbers.  Is this true? Convince me!</p>	<p><b>B3</b> What remainders are possible when you divide a square number by 4?</p>	<p><b>B4</b> Square an odd number then subtract 1.  Can you find any patterns?</p>
<p><b>C1</b> <math>a, b, c, d, e</math> are consecutive integers such that <math>a^2 + b^2 + c^2 = d^2 + e^2</math> Find <math>a, b, c, d,</math> and <math>e</math></p>	<p><b>C2</b> What is the smallest number, <math>n</math>, such that <math>n^2</math> is divisible by a square number greater than 4.</p>	<p><b>C3</b> People born in 1980 will be <math>n</math> years old in the year <math>n^2</math>. Find the value of <math>n</math>.</p>	<p><b>C4</b> Three <b>different</b> square numbers, <b>greater than 10</b>, are added together to make an odd number between 100 and 150.  How many ways are there to do this?</p>
<p><b>D1</b> <math>a, b, c, d, e</math> are consecutive integers such that <math>(a+b+c)^2 = (d+e)^2</math> Find <math>a, b, c, d,</math> and <math>e</math></p>	<p><b>D2</b> The product of two square numbers always equals a square number.  Is this true? Convince me!</p>	<p><b>D3</b> When I square an odd number, the answer is always odd.  Is this true? Convince me!</p>	<p><b>D4</b> What three-digit square numbers are also square numbers when their digits are reversed?</p>



## POWERS

### SQUARES OF INTEGERS

A spreadsheet is very useful to investigate or solve some of these problems

Ref: G1C1. **1E1**

<p><b>A1</b> What digits can a square number end with?</p> <p>0, 1, 4, 5, 6 or 9</p>	<p><b>A2</b> Find three square numbers which add together to make 142</p> <p>25 + 36 + 81</p>	<p><b>A3</b> Which two <b>consecutive</b> square numbers have a difference of 17</p> <p>81 and 64</p>	<p><b>A4</b></p> <p>1+49    9+49    16+64  1+81    9+81    25+49  4+64    16+36    36+64</p>
<p><b>B1</b> Split the numbers below into three groups so that each group adds up to a different square number:</p> <p>(2, 2)    (3, 3, 3, 3, 4)    ...  ... (4, 5, 5, 5, 6)</p>	<p><b>B2</b> False - only way to get an odd square number is if one of the prime numbers is 2.</p> <p>So 121 would have to be 2 + 119, but 119 is not prime!</p>	<p><b>B3</b> What remainders are possible when you divide a square number by 4?</p> <p>0 or 1</p>	<p><b>B4</b> Square an odd number then subtract 1.</p> <p>Can you find any patterns?</p> <p>You always get a multiple of eight.</p>
<p><b>C1</b> <math>a, b, c, d, e</math> are consecutive integers such that <math>a^2 + b^2 + c^2 = d^2 + e^2</math></p> <p>Find <math>a, b, c, d,</math> and <math>e</math></p> <p><math>10^2 + 11^2 + 12^2 = 13^2 + 14^2</math></p>	<p><b>C2</b> What is the smallest number, <math>n</math>, such that <math>n^2</math> is divisible by a square number greater than 4.</p> <p>3</p> <p>because <math>3^2</math> is divisible by 9</p>	<p><b>C3</b> People born in 1980 will be <math>n</math> years old in the year <math>n^2</math>.</p> <p>Find the value of <math>n</math>.</p> <p><math>n = 45</math></p> <p>because <math>45^2 = 2025</math></p>	<p><b>C4</b></p> <p>16+25+64    16+49+64  16+25+100    25+36+64  16+36+49    36+49+64  16+36+81</p>
<p><b>D1</b> <math>a, b, c, d, e</math> are consecutive integers such that <math>(a+b+c)^2 = (d+e)^2</math></p> <p>Find <math>a, b, c, d,</math> and <math>e</math></p> <p><math>(4 + 5 + 6)^2 = (7 + 8)^2</math></p>	<p><b>D2</b> True - if the two square numbers were <math>a^2</math> and <math>b^2</math></p> <p><math>a^2 \times b^2 = a \times a \times b \times b</math>  <math>= a \times b \times a \times b</math>  <math>= (a \times b)^2</math></p>	<p><b>D3</b> True - let <math>n</math> be even. This means that <math>n+1</math> is odd</p> <p><math>(n+1)^2 = n^2 + 2n + 1</math></p> <p>The +1 at the end means the answer is odd!</p>	<p><b>D4</b></p> <p>121  144 and 441  169 and 961  484  676</p>