STRENGTMEN

## SURDS

MULTIPLYING TWO-PART SURDS

## NO CALCULATOR

| A1 <br> Expand $\sqrt{2} \times(3+\sqrt{2})$ <br> Give your answer in the form $a+b \sqrt{2}$ where $a$ and $b$ are integers. | A2 <br> Expand $\sqrt{3} \times(7-\sqrt{3})$ <br> Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers. | A3 <br> Expand $\sqrt{2} \times(3+2 \sqrt{2})$ <br> Give your answer in the form $a+b \sqrt{2}$ where $a$ and $b$ are integers. | A4 <br> Expand $\sqrt{3} \times(5+4 \sqrt{3})$ <br> Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers. |
| :---: | :---: | :---: | :---: |
| B1 <br> Expand $(5+\sqrt{2})(2+\sqrt{2})$ <br> Give your answer in the form $a+b \sqrt{2}$ where $a$ and $b$ are integers. | B2 <br> Expand $(2+\sqrt{3})(5-\sqrt{3})$ <br> Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers. | B3 <br> Expand $(4+\sqrt{3})(1+2 \sqrt{3})$ <br> Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers. | B4 <br> Expand $(3-\sqrt{5})(2-2 \sqrt{5})$ <br> Give your answer in the form $a+b \sqrt{5}$ where $a$ and $b$ are integers. |
| C1 <br> Expand $(1+\sqrt{5})^{2}$ <br> Give your answer in the form $a+b \sqrt{5}$ where $a$ and $b$ are integers. | C2 <br> Expand $(3+\sqrt{7})^{2}$ <br> Give your answer in the form $a+b \sqrt{7}$ where $a$ and $b$ are integers. | C3 <br> Expand $(6-\sqrt{3})^{2}$ <br> Give your answer in the form $a+b \sqrt{3}$ where $a$ and $b$ are integers. | C4 <br> Expand $(4+3 \sqrt{2})^{2}$ <br> Give your answer in the form $a+b \sqrt{2}$ where $a$ and $b$ are integers. |
| D1 <br> Expand $(1+\sqrt{2})(3+\sqrt{8})$ <br> Give your answer in the form $a+b \sqrt{2}$ where $a$ and $b$ are integers. | D2 <br> Expand $(7-\sqrt{5})(2+\sqrt{20})$ <br> Give your answer in the form $a+b \sqrt{5}$ where $a$ and $b$ are integers. | D3 Expand and simplify $(5+\sqrt{6})(5-\sqrt{6})$ | D4 <br> Expand and simplify $(3+2 \sqrt{5})(\sqrt{20}-3)$ |

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| A1 $\text { Expand } \begin{aligned} \sqrt{2} & \times(3+\sqrt{2}) \\ & =3 \sqrt{2}+2 \\ & =2+3 \sqrt{2} \end{aligned}$ | A2 $\text { Expand } \begin{aligned} & \sqrt{3} \times(7-\sqrt{3}) \\ & =7 \sqrt{3}-3 \\ & =-3+7 \sqrt{3} \end{aligned}$ | A3 $\text { Expand } \begin{aligned} \sqrt{2} \times & (3+2 \sqrt{2}) \\ = & 3 \sqrt{2}+2 \times 2 \\ = & 4+3 \sqrt{2} \end{aligned}$ | A4 $\text { Expand } \begin{aligned} \sqrt{3} & \times(5+4 \sqrt{3}) \\ = & 5 \sqrt{3}+4 \times 3 \\ = & 12+5 \sqrt{3} \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| B1 $\begin{aligned} \text { Expand } & (5+\sqrt{2})(2+\sqrt{2}) \\ & F \quad 0 \quad I \\ = & 10+5 \sqrt{2}+2 \sqrt{2}+2 \\ = & 12+7 \sqrt{2} \end{aligned}$ | B2 $\begin{aligned} & \text { Expand }(2+\sqrt{3})(5-\sqrt{3}) \\ & F \text { F } \\ &=10-2 \sqrt{3}+5 \sqrt{3}-3 \\ &= 7+3 \sqrt{3} \end{aligned}$ | B3 $\begin{aligned} \text { Expand } & (4+\sqrt{3})(1+2 \sqrt{3}) \\ & F \\ = & 4+8 \sqrt{3}+\sqrt{3}+2 \times 3 \\ = & 10+9 \sqrt{3} \end{aligned}$ | B4 $\begin{aligned} & \text { Expand }(3-\sqrt{5})(2-2 \sqrt{5}) \\ & F \\ &= 6-6 \sqrt{5}-2 \sqrt{5}+2 \times 5 \\ &= 16-8 \sqrt{5} \end{aligned}$ |
| C1 $\text { Expand } \begin{aligned} & (1+\sqrt{5})^{2} \\ = & (1+\sqrt{5})(1+\sqrt{5}) \\ = & 1+\sqrt{5}+\sqrt{5}+5 \\ = & 6+2 \sqrt{5} \end{aligned}$ | C2 $\text { Expand } \begin{aligned} & (3+\sqrt{7})^{2} \\ = & (3+\sqrt{7})(3+\sqrt{7}) \\ = & 9+3 \sqrt{7}+3 \sqrt{7}+7 \\ = & 16+6 \sqrt{7} \end{aligned}$ | C3 $\begin{aligned} \text { Expand } & (6-\sqrt{3})^{2} \\ = & (6-\sqrt{3})(6-\sqrt{3}) \\ = & 36-6 \sqrt{3}-6 \sqrt{3}+3 \\ = & 39-12 \sqrt{3} \end{aligned}$ | C4 $\begin{aligned} \text { Expand } & (4+3 \sqrt{2})^{2} \\ = & (4+3 \sqrt{2})(4+3 \sqrt{2}) \\ = & 16+12 \sqrt{2}+12 \sqrt{2}+9 \times 2 \\ = & 34+24 \sqrt{2} \end{aligned}$ |
| D1 $\text { Expand } \begin{aligned} & (1+\sqrt{2})(3+\sqrt{8}) \\ = & 3+\sqrt{8}+3 \sqrt{2}+\sqrt{16} \\ = & 3+2 \sqrt{2}+3 \sqrt{2}+4 \\ = & 7+5 \sqrt{2} \end{aligned}$ | D2 $\begin{aligned} \text { Expand } & (7-\sqrt{5})(2+\sqrt{20}) \\ = & 14+7 \sqrt{20}-2 \sqrt{5}-\sqrt{100} \\ = & 14+7 \times 2 \sqrt{5}-2 \sqrt{5}-10 \\ = & 4+12 \sqrt{5} \end{aligned}$ | D3 <br> Expand and simplify $\begin{aligned} (5+\sqrt{6}) & (5-\sqrt{6}) \\ & =25-5 \sqrt{6}+5 \sqrt{6}-6 \\ & =19 \end{aligned}$ | D4 $\begin{aligned} & (3+2 \sqrt{5})(\sqrt{20}-3) \\ & =3 \sqrt{20}-9+2 \sqrt{100}-6 \sqrt{5} \\ & =3 \times 2 \sqrt{5}-9+2 \times 10-6 \sqrt{5} \\ & =11 \end{aligned}$ |

